

Meeting: 1006, Lubbock, Texas, SS 3A, Special Session on Classical and Differential Galois Theory

1006-16-161 **David J Saltman*** (saltman@math.utexas.edu), The University of Texas at Austin,
Mathematics Department, 1 University Station C1200, Austin, TX 78712-0257. *Cyclic Algebras
over p -adic Curves.*

Let Q_p be the p -adic field and K the function field of a curve over Q_p . It is useful to view K as the function field of a surface, projective over the p -adic integers \mathbf{Z}_p . In previous work the author showed that as long as q is prime to p , any division algebra D of order q in the Brauer group has degree bounded by q^2 . As part of the proof, one sees that often one has shown, when q is prime, that D is a crossed product. Thus one is interested in degree q ($q \neq p$ prime) division algebras over K . We show they are all cyclic. Along the way, we initiate a geometric study of ramification in dimensions larger than 1, and we will conjecture about what may be true over general surfaces and even general fields. (Received February 14, 2005)