

1007-20-205

**Igor Mineyev\*** ([mineyev@math.uiuc.edu](mailto:mineyev@math.uiuc.edu)), Department of Mathematics, University of Illinois at Urbana-Champaign, 250 Altgeld Hall, 1409 W. Green Street, Urbana, IL 61801. *Symmetric join functor.*

I will describe the functor  $\ast$  that associates to every metric space  $X$  its **symmetric join**  $\ast X$ .

(Here is how these symbols were typed: <http://www.math.uiuc.edu/~mineyev/math/art/symbols.pdf>)

$\ast X$  is a natural union of intervals connecting pairs of points in  $X$ , and it possesses a natural metric so that the inclusion  $X \hookrightarrow \ast X$  is an isometric embedding. The functor  $\ast$  applies to any metric space.

In a joint work with G. Yu a “nice” metric  $\hat{d}$  on a hyperbolic group was constructed. When applied to a hyperbolic group or graph with the metric  $\hat{d}$ , the symmetric join extends to the ideal boundary. This gives rise to a geodesic flow space with sharp properties which is an analog of the (total space of) the unit tangent bundle in hyperbolic manifolds. The above constructions allow avoiding ”quasi”-language in hyperbolic groups. (Received February 21, 2005)