

1007-57-226

Jay J Zimmerman* (jzimmerman@towson.edu), Department of Mathematics, Towson University, 8000 York Road, Towson, MD 21252. *The genus distribution for odd order groups.*

Suppose that G is an odd order group with symmetric genus of the form $2^k + 1$ for an integer k or $p + 1$ for an odd prime p . Then G is the semidirect product of Z_m by Z_n , where m and n are relatively prime. The genus action is given by a triangle group $\Gamma(r, s, t)$ satisfying the condition $|G| = lcm(r, s, t)$, except if G is the image of $\Gamma(5, 5, 5)$ with genus $p + 1$ for $p \equiv 1 \pmod{10}$. Unfortunately, there is no general relationship between the genus σ and the integers m and n . However, in the case, Z_n has a Sylow p -subgroup, that acts fixed point freely on Z_m and G is not the image of $\Gamma(5, 5, 5)$, then m and n satisfy the equation

$$\sigma = \left(\frac{m-1}{2} \right) (n-2).$$

It is easy to show that for an odd order group G with genus of the form $g = p + 1$, the order of G satisfies $2(g-1) \leq |G| \leq 5(g-1)$. The metacyclic groups with odd order smaller than 1000 all have Sylow subgroups of Z_n acting fixed point freely on Z_m . Thus for $g < 200$ of the form $p + 1$, we can decide if g is the genus of any odd order group. (Received February 22, 2005)