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An affinographic hyperplane arrangement is a finite set of hyperplanes in \mathbb{R}^n whose equations have the form $x_j - x_i = c$. The Shi and Linial arrangements are examples. The problem of determining the characteristic polynomial $p(\lambda)$ of such an arrangement can be solved (as, in effect, Athanasiadis did) by taking a large positive integer m and counting the number $\chi(m)$ of lattice points $x \in \mathbb{Z}_{>0}^n$ with all $x_i \leq m$ for large positive integers m . (Athanasiadis' method was a slightly complicated variant of this.) When m is large, $\chi(m) = p(m)$, a polynomial. However, for all $m > 0$, $\chi(m)$ is a piecewise polynomial and a Tutte invariant. We show the exact form of $\chi(m)$, from which it is apparent why it is a polynomial when m is large. Our method is to reinterpret the problem as one of coloring rooted integral gain graphs. (Received June 07, 2005)