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**Dhruv Mubayi** and **Yi Zhao\*** (yizhao@mathstat.gsu.edu), Department of Mathematics & Statistics, Georgia State University. *On the VC-dimension of Uniform Hypergraphs.*

In the early 70's, Sauer, Perles-Shelah, Vapnik-Chervonenkis independently proved that if a set system  $\mathcal{F}$  on  $[n]$  contains more than  $\binom{n}{0} + \dots + \binom{n}{d-1}$  sets, then there exists a *shattered*  $d$ -element set  $S$  of  $[n]$ , namely,  $\{E \cap S : E \in \mathcal{F}\}$  contains all subsets of  $S$ . Using the algebraic method, Frankl and Pach showed that for  $r$ -uniform  $\mathcal{F}$  ( $r \geq d$ ), the same holds whenever  $\mathcal{F} > \binom{n}{d-1}$  and conjectured that  $\mathcal{F} > \binom{n-1}{d-1}$  suffices. But this was later disproved by Ahlswede and Khachatrian. In this talk, we show that if  $d = 2^t + 1$  for positive integer  $t$ , then every  $d$ -uniform  $\mathcal{F}$  on  $[n]$  of size  $\binom{n}{d-1} - \lg n$  forces a shattered  $d$ -element set. We also note that there are infinite many constructions achieving the same effect as the one of Ahlswede and Khachatrian. (Received August 08, 2005)