

1009-33-121

**Martin E Muldoon\*** (muldoon@yorku.ca), Department of Mathematics and Statistics, York University, Toronto, Ontario M3J 1P3, Canada. *Continuous ranking of zeros of special functions*. Preliminary report.

Á. Elbert and A. Laforgia, *SIAM J. Math. Anal.* **15** (1984), 206–212, described a way in which the zeros of cylinder functions  $\mathcal{C}_\nu(x) = \cos \alpha J_\nu(x) - \sin \alpha Y_\nu(x)$  may be defined as functions of two variables  $\nu$  and  $\kappa$ , where  $\kappa$  is a kind of generalized rank. Specifically, when  $\nu > -1$ , the  $k$  th positive zero  $c(\nu, k, \alpha)$  of  $\mathcal{C}_\nu(x)$  has the property that the variables  $\alpha$  and  $k$  are not really independent but may be subsumed in the single variable  $\kappa = k - \alpha/\pi$ . Following Elbert and Laforgia, we write  $j_{\nu\kappa} = c(\nu, k, \alpha)$ . For integer values of  $\kappa$ ,  $j_{\nu\kappa}$  gives the zeros of  $J_\nu(x)$  while the values  $\kappa = k + \frac{1}{2}$  give the zeros of  $Y_\nu(x)$ . Here we extend this set of ideas to solutions of a general class of differential equations by showing that the notion of continuous rank of a zero follows naturally from the notion of “first phase” as described in the work of O. Borůvka. This enables us to derive a number of results on monotonicity properties of zeros of Bessel and Hermite functions. (Received August 10, 2005)