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28223. *Classifying prime ideals in Prüfer domains.*

For a nonzero prime ideal  $P$  of an integral domain  $R$  with quotient field  $K$ , set  $\Theta(P) = K$  if  $P$  is in the Jacobson radical of  $R$ , otherwise set  $\Theta(P) = \cap R_M$  where the  $M$  range over the maximal ideals that do not contain  $P$ . We consider five basic properties  $P$  may or may not have.  $P$  could be sharp:= [ $R_P$  does not contain  $\Theta(P)$ ]; antesharp:= [each maximal ideal of  $(P : P)$  that contains  $P$ , contracts to  $P$  in  $R$ ]; divisorial:= [ $P = (R : (R : P))$ ]; branched:= [proper  $P$ -primary ideals exist]; idempotent:= [ $P = P^2$ ]. Set  $\Lambda(P) = \langle V, W, X, Y, Z \rangle$  with the values of  $V, W, X, Y, Z$  reflecting whether  $P$  is, respectively, sharp/not sharp, antesharp/not antesharp, divisorial/not divisorial, branched/unbranched, idempotent/not idempotent. If  $R$  is a Prüfer domain we show that there are exactly twelve attainable values for  $\Lambda(P)$  when  $P$  is not maximal, and six values when  $P$  is maximal. (Received August 08, 2005)