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**Shane P. Redmond\*** ([Shane.Redmond@eku.edu](mailto:Shane.Redmond@eku.edu)), Eastern Kentucky University, 313 Wallace, 521 Lancaster Ave., Richmond, KY 40475. *Zero-Divisor Graphs of Finite Commutative Rings with Identity*. Preliminary report.

Let  $R$  be a commutative ring with (nonzero) identity. The zero-divisor graph of  $R$ , denoted  $\Gamma(R)$ , is the graph whose vertices are the nonzero zero-divisors of  $R$ , with two distinct vertices  $x$  and  $y$  adjacent if and only if  $xy = 0$ . The first half of this presentation uses  $\Gamma(R)$  to bound the cardinality of  $R$ , generalizing previous bounds. The second half discusses which graphs on  $n$  vertices can be realized as  $\Gamma(R)$ . A complete list of rings (up to isomorphism) for  $n = 1$  through 5 has been known. This is extended to  $n = 6$  through 14. An algorithm is given whereby, for *any* positive integer  $n$ , all zero-divisor graphs of *reduced* commutative rings with identity on  $n$  vertices are identified. (Received August 19, 2005)