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For a variety \mathcal{V} of algebras let $\mathbf{F}_{\mathcal{V}}(n)$ be the free algebra for \mathcal{V} on n free generators, let $f(n)$ denote the cardinality of $\mathbf{F}_{\mathcal{V}}(n)$ and let $c(n)$ be the cardinality of the congruence lattice of $\mathbf{F}_{\mathcal{V}}(n)$. The number of at most n -generated algebras in \mathcal{V} , up to isomorphism, is denoted by $g(n)$. In this talk we investigate the relationships between these functions in the case that \mathcal{V} is locally finite. Of particular concern is how close these three functions are to one another in the exponential hierarchy. Some sample results include: If $f(n)$ is an at least m -fold exponential function of n , then so is $c(n)$. If \mathcal{V} is a congruence distributive variety and $f(n)$ is at least m -fold exponential as a function of n , then $g(n)$ is at least $(m - 1)$ -fold exponential. Other results and open problems in this vein will be presented. (Received August 18, 2005)