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If \mathbf{A} is an algebra on a metric space $\langle A, d \rangle$ and if $\sigma \approx \tau$ is an equation of the appropriate type, then $\lambda_{\mathbf{A}}(\sigma, \tau)$ denotes the sup of $d(\sigma^{\mathbf{A}}(\mathbf{a}), \tau^{\mathbf{A}}(\mathbf{a}))$, with \mathbf{a} in the appropriate power of A . Let $\lambda_{\mathbf{A}}(\Sigma)$ be the sup of $\lambda_{\mathbf{A}}(\sigma, \tau)$ over all $(\sigma \approx \tau) \in \Sigma$, and let $\lambda_A(\Sigma)$ be the inf of $\lambda_{\mathbf{A}}(\Sigma)$ over all topological algebras \mathbf{A} (of the correct type) that are based on the space $\langle A, d \rangle$. If A is compatible with Σ , then $\lambda_A(\Sigma) = 0$, but the converse fails.

We shall mention some elementary results, examples and problems about $\lambda_A(\Sigma)$. In some cases, this quantity yields a conclusion sharper than non-compatibility: e.g., if A is $[0, 1]^2$ with the Euclidean metric, and Σ posits the existence of a one-one map $A^2 \rightarrow A$, then $\lambda_A(\Sigma) = 1/2\sqrt{2}$. We describe some attempts to base a useful topological invariant on λ . (Received August 30, 2005)