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**Louiza Fouli\*** (lfouli@math.purdue.edu), Department of Mathematics, 150 North University Street, West Lafayette, IN 47907-2067. *The core of ideals in arbitrary characteristic*. Preliminary report.

Let  $R$  be a Noetherian local ring with infinite residue field  $k$  and  $I$  an  $R$ -ideal. The core of  $I$ ,  $\text{core}(I)$ , is defined to be the intersection of all (minimal) reductions of  $I$ . Under some technical conditions (which are automatically satisfied in case  $I$  is equimultiple) Polini and Ulrich have shown that for a Gorenstein local ring,

$$J^{n+1} : I^n \subset \text{core}(I) \subset J^{n+1} : \sum_{y \in I} (J, y)^n$$

for  $n \gg 0$ , and  $J$  a minimal reduction of  $I$ . This holds in any characteristic. They also show that if  $\text{char } k = 0$  or  $\text{char } k \gg 0$ , then  $\text{core}(I) = J^{n+1} : I^n = J^{n+1} : \sum_{y \in I} (J, y)^n$  for  $n \gg 0$ . We present an example where  $\text{char } k = 2$  and  $\text{core}(I) \neq J^{n+1} : \sum_{y \in I} (J, y)^n$ . On the other hand, we show that if  $R$  is a positively graded Gorenstein reduced  $k$ -algebra ( $k$  an infinite perfect field) and  $I$  is an  $R$ -ideal generated by forms of the same degree then  $\text{core}(I) = J^{n+1} : I^n$  in any characteristic. Part of this work is joint with Claudia Polini and Bernd Ulrich.

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