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University of Regina, Regina, Sask. S4S 0A2, Canada. *On the Exponents of Oscillatory Matrices.*

A real matrix is called totally nonnegative (resp. totally positive) if all of its minors are nonnegative (resp. positive). An  $n \times n$  matrix is said to oscillatory if it is totally nonnegative and some positive integral power of it is totally positive. The exponent of an oscillatory matrix  $A$  is the smallest positive integer  $k$  such that  $A^k$  is totally positive. Gantmacher and Krein proved long ago that  $k \leq n - 1$ . We will present a new “combinatorial” proof of this result and describe the subclass of  $n \times n$  oscillatory matrices whose exponent is equal to  $n - 1$ . (Received August 18, 2005)