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Sivaram K. Narayan* (sivaram.narayan@cmich.edu), Department of Mathematics, Pearce Hall 111, Central Michigan University, Mount Pleasant, MI 48859. *The Minimum Positive Semi-definite Rank of a Graph.*

A matrix $A \in M_n(\mathbb{C})$ is called *Hermitian* if $A = A^*$. A Hermitian matrix with nonnegative eigenvalues is called a *positive semi-definite (PSD)* matrix. Given a Hermitian matrix A we associate a simple, undirected graph G with $V(G) = \{1, \dots, n\}$ and edges $E(G) = \{(i, j) \mid a_{ij} \neq 0, i \neq j\}$. The graph is independent of the diagonal entries of A . The *minimum positive semi-definite (PSD) rank* of G , denoted $msr(G)$, is the minimum rank of A where A varies over all PSD matrices with graph G .

In this talk we present results on the upper and lower bounds for the minimum PSD rank, and the effect of topological changes such as vertex or edge modifications on $msr(G)$. In addition, we will discuss the $msr(G)$ for some classes of graphs, including bipartite graphs and chordal graphs.

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