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Given a field  $F$  and an undirected graph  $G$  on  $n$  vertices, let  $S(F, G)$  be the set of all symmetric  $n \times n$  matrices over  $F$  whose nonzero off-diagonal entries occur in exactly the positions corresponding to the edges of  $G$ . Let  $\text{mr}(F, G)$  be the minimum rank of all matrices in  $S(F, G)$ . The graphs for which  $\text{mr}(F, G) \leq 2$  have been characterized in two ways and the description depends on whether or not  $F$  is finite or infinite and whether or not  $\text{char } F = 2$ .

This talk will discuss the characterization in terms of forbidden subgraphs. For example, there are 6 forbidden subgraphs for the class of graphs with  $\text{mr}(\mathbb{R}, G) \leq 2$  while, on the other extreme, there are 7 forbidden subgraphs for those with  $\text{mr}(F_2, G) \leq 2$ . The two lists have important similarities and differences. Finding a complete list of forbidden subgraphs for  $\text{mr}(F, G) \leq 3$  is much more difficult, although a result of G. Ding says that the list is finite if  $F$  is. We give a progress report on the forbidden subgraph list for  $F = F_2$  and  $F = \mathbb{R}$ . (Received August 26, 2005)