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**Jean-Camille Birget\*** (birget@camden.rutgers.edu), Dept. of Computer Science, Rutgers University at Camden, Camden, NJ 08102. *Algebraic characterizations of one-way functions*. Preliminary report.

One-way functions are a fundamental concept of cryptography. They are functions between words over a finite alphabet such that it is “easy” to compute  $f(x)$  on input  $x$ , but given  $y$  it is “extremely hard” to find any  $x$  such that  $f(x) = y$ . When  $f$  is a function between bit-strings of length  $n$ , we define “easy” to mean that  $f$  has a “small” acyclic digital circuit, and “extremely hard” to mean that all generalized inverses of  $f$  only have “very large” acyclic circuits. For all known reasonable definitions, it is an open problem whether one-way functions exist; the problem is related to P vs. NP.

We show that one-way permutations (between bit-strings of length  $n$ ) exist if and only if the symmetric group  $\mathfrak{S}_N$  (where  $N = 2^n$ ) has super-polynomial distortion as a subgroup of the symmetric monoid  $F_N$ , as a function of  $n$ . The generating sets here consist of fixed finite sets, together with the transpositions of bit positions. Instead of the infinite family  $\mathfrak{S}_N$  one can also use the Richard Thompson group  $V$  and the analogous monoid, and one can refine the result to finite generating sets. (Received August 03, 2005)