

1011-49-320

Mikil Foss* (mfoss@math.unl.edu), Department of Mathematics, Avery Hall, University of Nebraska-Lincoln, Lincoln, NE 68588-0130. *Global Lipschitz regularity of minimizers for asymptotically convex integrals.*

Suppose that $p > 2$ and $\Omega \subset \mathbb{R}^n$ with a smooth boundary. We say that a function $g \in C^2(\mathbb{R}^{N \times n}; \mathbb{R})$ is asymptotically convex if for each $\varepsilon > 0$, there exists a $\sigma_\varepsilon < +\infty$ such that

$$\left\| \frac{\partial^2}{\mathbf{F}^2} [\|\mathbf{F}\|^p] - \frac{\partial^2}{\mathbf{F}^2} g(\mathbf{F}) \right\| < \varepsilon \|\mathbf{F}\|^{p-2},$$

whenever $\|\mathbf{F}\| > \sigma_\varepsilon$. M. GIAQUINTA & G. MODICA (1986) and J. -P. RAYMOND (1991) established the local Lipschitz regularity for minimizers of functionals of the form

$$\mathbf{u} \mapsto \int_{\Omega} g(\nabla \mathbf{u}(\mathbf{x})) \, d\mathbf{x},$$

where g is asymptotically convex. It is not completely straightforward to extend this result up to the boundary of Ω , since the technique used relies on UHLENBECK's local regularity result for solutions to elliptic systems. I will present some global regularity results for minimizers of asymptotically convex integrals, including a global Lipschitz regularity result. (Received August 30, 2005)