

1011-68-292

**Jack H. Lutz\*** ([lutz@cs.iastate.edu](mailto:lutz@cs.iastate.edu)), Department of Computer Science, 226 Atanasoff Hall, Ames, IA 50011. *Dimensions of Copeland-Erdős Sequences*. Preliminary report.

The base- $k$  *Copeland-Erdős sequence* given by an infinite set  $A$  of positive integers is the infinite sequence  $CE_k(A)$  formed by concatenating the base- $k$  representations of the elements of  $A$  in numerical order. This talk concerns the *finite-state dimension*  $\dim_{\text{FS}}(CE_k(A))$ , the *finite-state strong dimension*  $\text{Dim}_{\text{FS}}\text{Dim}_{\text{FS}}(CE_k(A))$ , the *zeta-dimension*  $\text{Dim}_{\zeta}(A)$ , a kind of discrete fractal dimension discovered many times over the past few decades, and the *lower zeta-dimension*  $\dim_{\zeta}(A)$ , a dual of  $\text{Dim}_{\zeta}(A)$ . We prove the following.

1.  $\dim_{\text{FS}}(CE_k(A)) \geq \dim_{\zeta}(A)$ . This extends the 1946 proof by Copeland and Erdős that the sequence  $CE_k(\text{PRIMES})$  is Borel normal.
2.  $\text{Dim}_{\text{FS}}(CE_k(A)) \geq \text{Dim}_{\zeta}(A)$ .
3. These bounds are tight in the strong sense that these four quantities can have (simultaneously) any four values in  $[0, 1]$  satisfying the four above-mentioned inequalities.

This is joint work with Xiaoyang Gu and Philippe Moser. (Received August 30, 2005)