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Jeremy L Martin* (jmartin@math.ku.edu), Department of Mathematics, 405 Snow Hall, 1460 Jayhawk Boulevard, Lawrence, KS 66045-7523, and **David Savitt** and **Ted Singer**. *Harmonic algebraic curves and noncrossing partitions*. Preliminary report.

Let $f(z)$ be a complex polynomial, and let R and I be the sets $\{\operatorname{Re}(f(z)) = 0\}$ and $\{\operatorname{Im}(f(z)) = 0\}$, regarded as plane curves in \mathbb{R}^2 . As observed by Gauss (in his first proof of the Fundamental Theorem of Algebra), each of the curves R, I may be described topologically by a noncrossing matching. The pair of matchings thus obtained is a combinatorial invariant of the polynomial $f(z)$, called its *basketball*. We prove that every basketball is realized by some polynomial, and present several related problems for further study. (Received September 06, 2005)