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**Shrawan Kumar\*** ([shrawan@email.unc.edu](mailto:shrawan@email.unc.edu)), Department of Mathematics, UNC at Chapel Hill, Chapel Hill, NC 27599-3250. *On Cachazo-Douglas-Seiberg-Witten conjecture for simple Lie algebras*. Preliminary report.

Let  $g$  be a simple Lie algebra over the complex numbers. Consider the exterior algebra  $R := \wedge(g \oplus g)$  on two copies of  $g$ . There are three ‘standard’ copies of the adjoint representation  $g$  in the degree 2 component  $R^2$ . Let  $J$  be the (bigraded) ideal of  $R$  generated by the three copies  $C_1, C_2, C_3$  of  $g$  (in  $R^2$ ) and define the bigraded  $g$ -algebra  $A := R/J$ . The Killing form gives rise to a  $g$ -invariant  $S \in A^{1,1}$ .

Motivated by supersymmetric gauge theory, Cachazo-Douglas-Seiberg-Witten made the following conjecture.

(i) *The subalgebra  $A^g$  of  $g$ -invariants in  $A$  is generated, as an algebra, by the element  $S$ .*

(ii)  *$S^h = 0$ .*

(iii)  *$S^{h-1} \neq 0$ , where  $h$  is the dual Coxeter number.*

The aim of this work is to give a uniform proof of the above conjecture part (i). In addition, we give a conjecture, the validity of which would imply part (ii) of the above conjecture. (Received September 12, 2005)