

1012-42-134

Edward N. Wilson* (enwilson@math.wustl.edu), Department of Mathematics, Campus Box 1146, Washington University in St. Louis, One Brookings Drive, St. Louis, MO 63130, and

Kanghui Guo, Demetrio Labate, Wang Q Lim and Guido L. Weiss. BZ^n Invariant Spaces.

Let B be a countable subgroup of the group of $n \times n$ matrices with integer entries and determinant of modulus one. Then the semi-direct product BZ^n acts unitarily on $L^2(\mathbb{R}^n)$ by $\pi(b, k)f(x) = f(b^{-1}x - k)$ and a BZ^n invariant space is a closed π -invariant subspace. B is admissible if there exists a countable set $\{\phi_i : i \in \mathbb{N}\}$ such that $\{\pi(b, k)\phi_i : (b, k) \in BZ^n, i \in \mathbb{N}\}$ is a Parseval frame for $L^2(\mathbb{R}^n)$. If the right action of B on $\hat{\mathbb{R}}^n$ admits a measurable cross section for B -orbits, B is admissible and it's likely that this sufficient condition is also necessary. In the same way that ordinary wavelet theory rests on the properties of Z^n -invariant spaces, the theory of AB composite wavelets rests on the properties of BZ^n invariant spaces; to a remarkable extent, standard shift invariant space theorems and constructions have close BZ^n analogs. For example, in the case when A consists of powers of a single integer matrix a normalizing B , $|deta| \#(B/(aBa^{-1})) - 1$ is the number of generators for every AB orthonormal wavelet system. (Received September 16, 2005)