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C-Y. Jean Chan* (cchan@uark.edu), Department of Mathematics, University of Arkansas, Fayetteville, AR 72701, and **Claudia Miller** (cmille06@syr.edu), Department of Mathematics, Syracuse University, Syracuse, NY 13244. *An Application of the Riemann-Roch Formula in the Blow-up Algebra*. Preliminary report.

Let (A, \mathfrak{m}) be a regular local ring. The Rees algebra $A[\mathfrak{m}t]$ of A is the homogeneous ring of the blowup $X = \text{Proj } A[\mathfrak{m}t]$ of $\text{Spec } A$ at $\text{Spec}(A/\mathfrak{m})$. Let $P_M(t)$ be the Hilbert-Samuel polynomial of a finitely generated A -module M such that $P_M(n) = \ell(M/\mathfrak{m}^n M)$ for $n \gg 0$. The *Rees module* $R_{\mathfrak{m}}(M) = \bigoplus_{n \geq 0} \mathfrak{m}^n M$ of M is a graded module over $A[\mathfrak{m}t]$.

In graded cases, the Riemann-Roch formula relates the Euler characteristic of a graded module to its Chern characters. In this work, we apply the Grothendieck-Riemann-Roch theorem to the blow-up X of $\text{Spec } A$ and obtain an alternative formula which relates the Hilbert-Samuel polynomial $P_M(t)$ of M over the local ring A to the Chern characters of the graded Rees module $R_{\mathfrak{m}}(M)$ over the graded ring $A[\mathfrak{m}t]$. (Received February 06, 2006)