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**Eric T Sawyer\*** ([sawyer@mcmaster.ca](mailto:sawyer@mcmaster.ca)), Department of Mathematics and Statistics, McMaster University, Hamilton, Ontario L8s 4K1. *Regularity for certain subelliptic Monge-Ampère equations.*

Let  $u \in C^{1,1}(\Omega)$  be a convex solution to the generalized Monge-Ampère equation,  $\det D^2u = k(x, u, Du)$  with  $k$  smooth  $\approx (|x_1|^{2m} + \psi(x_1, \mathbf{x})) K(x, u, Du)$ , where  $K > 0, \psi \geq 0$  are smooth and  $\psi^{\frac{1}{2m}}$  Lipschitz. **Conjecture:** If  $d = \det \left[ \frac{\partial^2 u}{\partial x_i \partial x_j} \right]_{i,j=2}^n > 0$ , then  $u \in C^\infty(\Omega)$ .

P. Guan proved the conjecture in dimension  $n = 2$  using the classical partial Legendre transform. Subsequently, C. Rios, E. Sawyer and R. L. Wheeden generalized the partial Legendre transform to higher dimensions, and in dimension  $n \geq 3$ , used it to establish the conjecture under the additional regularity assumption  $u \in C^{2,1}(\Omega)$ . Here we relax the  $C^{2,1}$  assumption to  $u \in W^{3,q}(\Omega)$ ,  $q > \text{subelliptic dimension}$ , and in the special case  $\psi \equiv 0$ ,  $u \in W^{3,2}(\Omega) \cap C^2(\Omega)$ . This is part of ongoing work with C. Rios and R.L. Wheeden. (Received February 07, 2006)