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**Jie Xiao\*** (jxiao@math.mun.ca), Department of Mathematics and Statistics, Memorial University of Newfoundland, St. John's, NL A1C 5S7, Canada. *Towards  $Q$ -Extension of  $BMO$  by Quadratic Campanato-Morrey Space and Incompressible Navier-Stokes System.* Preliminary report.

In this talk, we will show: for  $\alpha \in (0, 1)$ ,  $Q_\alpha(\mathbb{R}^n)$ , not only as an intermediate space of  $W^{1,n}(\mathbb{R}^n)$  and  $BMO(\mathbb{R}^n)$  but also as a conformal variant of Sobolev space  $\dot{L}_\alpha^2(\mathbb{R}^n)$  which is sharply imbedded in  $L^{\frac{2n}{n-2\alpha}}(\mathbb{R}^n)$ , is isomorphic to a quadratic Campanato-Morrey space under fractional differentiation; at the same time, the dot product  $\nabla \cdot (Q_\alpha(\mathbb{R}^n))^n$  can be applied to derive the well-posedness of the scaling invariant mild solutions of the incompressible Navier-Stokes system in  $\mathbb{R}_+^{1+n} = (0, \infty) \times \mathbb{R}^n$ . (Received February 02, 2006)