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Let C be a smooth closed curve of length 2π in \mathbb{R}^3 , and let $\kappa(s)$ be its curvature, regarded as a function of arc length. We associate with this curve the one-dimensional Schrödinger operator $H_C = -d^2/ds^2 + \kappa^2$ acting on the space of square integrable 2π -periodic functions. A natural conjecture is that the lowest spectral value $e(C)$ is bounded below by 1 for any curve (this value is assumed when C is a circle). We study a family of curves that includes the circle and for which $e(C) = 1$ as well. We show that the curves in this family are local minimizers, i.e., $e(C)$ can only increase under small perturbations leading away from the family. (Received February 06, 2006)