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IL 60208. *Associative Submanifolds of a G_2 Manifold.*

McLean showed that the space $\mathcal{A}(M)$ of Associative submanifolds of an integrable G_2 manifold (M, φ) , in a neighborhood of a fixed one $Y \subset (M, \varphi)$, can be identified with the kernel of the Dirac operator on the normal bundle $\mathcal{D} : \Omega^0(\nu) \rightarrow \Omega^0(\nu)$. Hence $\mathcal{A}(M)$ is not smooth and the deformation space of Y is obstructed. We generalize this theorem to non-integrable (M, φ) case, and then relate this to pseudo-associative deformations of Y (where φ is also allowed to move, or alternatively allow that, only after rotating the tangent planes by a fixed element the gauge group, they be associative). By using this we can perturb $\mathcal{A}(M)$ to a smooth object, infinitesimally this has an affect of changing \mathcal{D} to a twisted Dirac operator \mathcal{D}_A , twisted by some connection A in ν . We will discuss ways of obtaining compactness by cutting this perturbed object with some additional equations.

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