

1016-03-212

**Karen M. Lange\*** ([klange@math.uchicago.edu](mailto:klange@math.uchicago.edu)), Mathematics Department, University of Chicago, 5734 S. University Ave., Chicago, IL 60637. *Degree Spectra of Homogeneous Models.*

Following Goncharov, Peretyat'kin, Millar, and others, we study the degree spectrum of a fixed nontrivial homogeneous model satisfying minimal computability conditions. Relativizing the conditions for the Goncharov-Peretyat'kin Effective Extension Property, we say a model  $\mathcal{A}$  has a  $\mathbf{d}$ -basis of types if the types realized in  $\mathcal{A}$  are all computable and  $\mathbf{d}$  can list  $\Delta_0$  indices for all types realized in  $\mathcal{A}$ . Goncharov, Millar, and Peretyat'kin showed that there exists a homogeneous model  $\mathcal{A}$  with a  $\mathbf{0}$ -basis such that  $\mathbf{0} \notin dSp^e(\mathcal{A})$ .

We prove that for a countable homogeneous  $\mathcal{A}$  with a  $\mathbf{0}'$ -basis,  $dSp^e(\mathcal{A})$  always contains a low degree. We call a degree  $\mathbf{d}$   *$\mathbf{0}$ -homogeneous bounding* if  $\mathbf{d} \in dSp^e(\mathcal{A})$  for all nontrivial homogeneous models  $\mathcal{A}$  with  $\mathbf{0}$ -bases. We show that the  $\text{nonlow}_2 \Delta_2^0$  degrees exactly characterize the  $\mathbf{0}$ -homogeneous bounding degrees below  $\mathbf{0}'$ . Finally, given a homogeneous model  $\mathcal{A}$  with a  $\mathbf{0}$ -basis, we show that if the theory  $T$  of  $\mathcal{A}$  has all types computable, then  $dSp^e(\mathcal{A})$  contains all non-zero degrees. (Received February 13, 2006)