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A Hermitian form  $q$  on the dual space,  $\mathfrak{g}^*$ , of the Lie algebra,  $\mathfrak{g}$ , of a Lie group,  $G$ , determines a Laplacian,  $\Delta$ , on  $G$ . It will be shown that Hörmander's condition for hypoellipticity of the Laplacian holds if and only if the associated Hermitian form, induced by  $q$  on the dual of the universal enveloping algebra, is nondegenerate. The subelliptic heat semigroup,  $e^{t\Delta/4}$ , is given by convolution by a  $C^\infty$  probability density  $\rho_t$ . Analogous to earlier work in the strongly elliptic case, we are able to show that if  $G$  is complex, connected, and simply connected then the Taylor expansion defines a unitary map from the space of holomorphic functions in  $L^2(G, \rho_t)$  onto (a subspace of) the dual of the universal enveloping algebra in the norm induced by  $q$ . (Received February 13, 2006)