

1016-32-274

**Frederico Xavier\*** (xavier.1@nd.edu), 255 Hurley Hall, Notre Dame, IN 46556. *Rigidity of the Identity.*

The structure of the group  $\text{Aut}(\mathbb{C}^n)$  of biholomorphisms of  $\mathbb{C}^n$  is largely unknown if  $n > 1$ . For instance, the still unsettled jacobian conjecture claims that  $\text{Aut}(\mathbb{C}^n)$  contains all polynomial local biholomorphisms. In stark contrast  $\text{Aut}(\mathbb{C})$  is rather small, consisting of the non-constant affine linear maps. The description of  $\text{Aut}(\mathbb{C})$  follows from the observation that an injective holomorphic function  $f : \mathbb{C} \rightarrow \mathbb{C}$  satisfying  $f(0) = 0$  and  $f'(0) = 1$  must be the identity. These considerations suggest that similar characterizations of the identity might be useful in understanding the structure of  $\text{Aut}(\mathbb{C}^n)$ . Using (real) geometric methods we prove that an injective holomorphic map  $f : \mathbb{C}^n \rightarrow \mathbb{C}^n$  is the identity  $I$  if and only if the power series at 0 of  $f - I$  has no terms of order  $\leq 2n + 1$  and the function  $|\det Df(z)| |z|^{2n} |f(z)|^{-2n}$  is subharmonic throughout  $\mathbb{C}^n$ . (Received February 14, 2006)