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Thomas H. Mac Gregor* (pemaquid@lincoln.midcoast.com), 61 Riverview Road, Pemaquid, ME 04558. *Fractional Cauchy Transforms and Compositions, Preliminary Report*. Preliminary report.

For $\alpha > 0$ let \mathcal{F}_α denote the Banach space of fractional Cauchy transforms defined in the open unit disk D . We discuss the question of when the composition of $f \mapsto \circ\varphi$ is a continuous linear operator on \mathcal{F}_α , where $\varphi : D \rightarrow D$ is analytic. A known result is that this happens for every such φ when $\alpha \geq 1$. This is not generally true when $0 < \alpha < 1$.

We show that if the Taylor series for φ' is absolutely convergent the question has a positive answer for all $\alpha > 0$. This also happens if φ is univalent, $\sup \{|\varphi(z)| : |z| < 1\} < 1$ and $\alpha > 1/2 - 1/320$. (Received February 02, 2006)