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**Oleg Eroshkin\*** ([oleg.eroshkin@unh.edu](mailto:oleg.eroshkin@unh.edu)), Department of Mathematics and Statistics,  
Kingsbury Hall, University of New Hampshire, Durham, NH 03824. *Pluripolarity of manifolds of  
Gevrey class and asymptotics of  $n$ -width.*

Let  $D$  be a bounded domain in  $\mathbb{C}^m$  containing a compact set  $K$ . We consider the compact set  $A_K^D \subset C(K)$  of continuous functions  $f$  that allow holomorphic extensions to  $D$  satisfying the inequality  $\|f\|_D \leq 1$ .

We study how the “massiveness” of  $A_K^D$  is related to geometric properties of  $K$ . It is the standard approach to characterize the “massiveness” of compacts by means of  $n$ -width or  $\varepsilon$ -entropy, introduced by A. N. Kolmogorov.

We define Kolmogorov dimension of  $K$  in terms of asymptotic behavior of  $n$ -width (or  $\varepsilon$ -entropy) of  $A_K^D$ . This notion is related to pluripotential properties of  $K$ . If Kolmogorov dimension of compact  $K \subset \mathbb{C}^m$  less than  $m$ , then  $K$  is pluripolar.

E. Bedford proved that real-analytic non-generic manifolds are pluripolar. Recently D. Coman, N. Levenberg and E. Poletsky proved that curves of appropriate Gevrey class are pluripolar. We generalize these results to non-generic manifolds of Gevrey class, estimate the Kolmogorov dimensions of such manifolds and show that these estimates are sharp. (Received December 30, 2005)