A CPR-graph is a graph associated with a permutation representation of a C-group (that is, the automorphism group of a regular polytope). We study a number of problems about regular polytopes that can be attacked by using CPR-graphs. In particular, we explain how polyhedra can be constructed that have alternating groups as automorphism groups. (Received February 21, 2006)