

1019-46-115

**Jack Spielberg\*** ([jack.spielberg@asu.edu](mailto:jack.spielberg@asu.edu)), Department of Mathematics & Statistics, Arizona State University, P. O. Box 871804, Tempe, AZ 85287-1804. *A dynamical restriction on  $C^*$ -algebras of graphs.*

It is known that for any countable abelian group  $G$  there is an (irreducible) graph whose  $C^*$ -algebra has trivial  $K_1$ , and  $K_0$  equal to  $G$ . One can arrange that  $K_1$  be a given free abelian group, but graph  $C^*$ -algebras are inherently limited to having free  $K_1$ . We describe another inherent limitation on the possible  $K$ -theory of graph  $C^*$ -algebras, imposed by automorphisms of the  $K$ -theory. Consider a (countable) abelian group  $G$  with subgroup  $H$ , and an automorphism  $f$  of  $G$  having prime order  $p$  and leaving  $H$  invariant. Then the following two conditions are equivalent:

1. There is a graph  $E$  with subgraph  $F$ , and an order  $p$  automorphism  $g$  of  $E$  leaving  $F$  invariant, such that  $C^*(F)$  is a subalgebra of  $C^*(E)$ ,  $K_1 = 0$  for both algebras,  $K_0$  induces the containment of  $H$  in  $G$ , and  $g$  defines an (order  $p$ ) automorphism of  $C^*(E)$  that induces  $f$  in  $K$ -theory.
2.  $[(f - id)G] \cap H = (f - id)H$ .

In particular, we give simple examples of inclusions of groups for which no such graphs can exist. (Received August 10, 2006)