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Eulalia Nualart* (nualart@math.utah.edu), University of Utah, Department of Mathematics, 155 S 1400 E, JWB 118, Salt Lake city, UT 84112. *Hitting probabilities for systems of non-linear stochastic heat equations.*

In this talk we develop potential theory for a system of d non-linear stochastic heat equations in spatial dimension 1 driven by d -dimensional space-time white noise. Using techniques of Malliavin calculus, we establish upper and lower bounds on the one-point density of the solution $u(t, x)$, and upper bounds of Gaussian-type on the two-point density of $(u(s, y), u(t, x))$. In particular, this estimate quantifies how this density degenerates as $(s, y) \rightarrow (t, x)$. From these results, we deduce upper and lower bounds on hitting probabilities of the process $(u(t, x), t \in \mathbb{R}_+, x \in [0, 1])$, in terms of respectively Hausdorff measure and Newtonian capacity. These estimates make it possible to show that points are polar when $d \geq 7$ and are not polar when $d \leq 5$. We also show that the Hausdorff dimension of the range of the process is 6 when $d > 6$. Finally, we obtain the values of the Hausdorff dimensions of the level sets of these processes. (Received August 09, 2006)