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**Art M Duval, Caroline Klivans and Jeremy L Martin\*** (jmartin@math.ku.edu),  
Department of Mathematics, 405 Snow Hall, 1460 Jayhawk Boulevard, Lawrence, KS 66045. *A  
simplicial matrix-tree theorem.* Preliminary report.

Building upon the work of G. Kalai and R. Adin, we extend the concept of a spanning tree from graphs to simplicial complexes. For all complexes  $\Delta$  satisfying a mild technical condition, we show that the simplicial spanning trees of  $\Delta$  can be enumerated using its Laplacian matrices, generalizing the matrix-tree theorem. As in the graphic case, replacing the Laplacian with a weighted analogue yields more refined combinatorial information about simplicial spanning trees. There is strong evidence that the resulting weighted tree enumerator factors nicely when  $\Delta$  is a shifted or matroid complex. (Received August 17, 2006)