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Triangulations of a convex polygon are known to be counted by the Catalan numbers. A natural generalization of a triangulation is a  $k$ -triangulation, which is defined to be a maximal set of diagonals so that no  $k + 1$  of them mutually cross in their interiors. It was proved by Jonsson that  $k$ -triangulations are enumerated by certain determinants of Catalan numbers, that are also known to count  $k$ -tuples of non-crossing Dyck paths.

There are several simple bijections between triangulations of a convex  $n$ -gon and Dyck paths. However, no bijective proof of Jonsson's result is known for general  $k$ . Here we solve this problem for  $k = 2$ , that is, we present a bijection between 2-triangulations of a convex  $n$ -gon and pairs  $(P, Q)$  of Dyck paths of semilength  $n - 4$  so that  $P$  never goes below  $Q$ . The bijection is obtained by constructing isomorphic generating trees for the sets of 2-triangulations and pairs of non-crossing Dyck paths. (Received August 03, 2006)