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H. Vic Dannon* (vick@adnc.com), CA. *Riemann Hypothesis Proof.*

In 1859, Riemann derived the functional equation $\xi(z) = \xi(1 - z)$ that defines his $\zeta(z)$ as analytic function in $z \neq 1$.

In $x > 1$, $\zeta(z)$ equals $\sum 1/n^z$.

For $x > 0$, Riemann proved $\xi(z) = \lim_{N \rightarrow \infty} \int_{t=0}^{t=\infty} \left(\sum_{n=1}^N e^{-n^2\pi t} \right) t^{\frac{1}{2}z-1} dt$. But his derivation was misinterpreted as a proof of his functional equation. In that confusion, the formula was lost. We supply a detailed proof of it.

Riemann claimed that all the zeros of $\zeta(z)$ in $0 < x < 1$, are on the line $x = \frac{1}{2}$.

Put $|\xi(z)| \equiv \varphi(z)$, and let $0 < \alpha < \frac{1}{2}$. We use Riemann's formula to show that $\varphi(\frac{1}{2} - \alpha + iy_0)$ is decreasing.

Thus, $\zeta(\frac{1}{2} - \alpha_0 + iy_0) = 0$ implies $0 = \varphi(\frac{1}{2} - \alpha_0 + iy_0) \geq \varphi(\frac{1}{2} - \alpha + iy_0) \geq 0$, for all $0 < \alpha < \alpha_0$, and then $\zeta(z) \equiv 0$.

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