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David E Speyer* (speyer@umich.edu), Department of Mathematics, 2074 East Hall, 530 Church Street, Ann Arbor, MI 48105. *Matroid Invariants and K-Theory*.

Let x be a point of the Grassmannian $G(d, n)$. The matroid of x consists of the data of which of the Plücker coordinates of x are zero. Experience has shown that this data captures the “combinatorial features” of x and matroid theorists have found many productive numerical and polynomial invariants to associate to x .

Let T be the torus $(\mathbb{C}^*)^n$ acting on $G(d, n)$ and let $\overline{T}x$ be the closure of the T orbit through x . The class of the structure sheaf of $\overline{T}x$ in $K_0(G(d, n))$ depends only on the matroid of x . As I will explain, a number of well known matroid invariants are, either provably or conjecturally, the result of applying linear functions on $K_0(G(d, n))$ to the structure sheaf of $\overline{T}x$. I will describe how, by considering K -theory I found a new matroid invariant, which behaves nicely under the operations of matroid duality, direct sum, two-sum and series-parallel extension. Using this invariant, I was able to show that if x_{gen} is a generic point of $G(d, n)$ and T_0 is the limit of a T -equivariant degeneration of $\overline{T}x_{\text{gen}}$ then T_0 contains at most $(n - c - 1)!/(d - c)!(n - d - c)!(c - 1)!$ strata of dimension $n - c$.

I will not assume prior knowledge of K -theory. (Received September 04, 2006)