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The Weingarten Curvature Problem: Prescribing Gauss-Kronecker on Group Invariant Convex Hypersurfaces.

We consider the problem of the existence of a hypersurface in \mathbb{R}^{n+1} with prescribed Gauss-Kronecker curvature on radial directions: Given a positive G -invariant function F , defined on $\mathbb{R}^{n+1} \setminus \{0\}$, where $G \subset O(n+1)$ is fixed point free subgroup, we examine the existence of a hypersurface M , star-shaped about the origin, satisfying that its Gauss-Kronecker curvature is given by $F|_M$.

This problem may be viewed in the setting of second order fully nonlinear elliptic partial differential equations, in particular it is of Monge-Ampere type. We may use a topological degree theory argument to solve this problem under certain assumptions on F , which are geometrically natural, and generalizations of the case when F is bounded between two constants. In particular, we require that $\limsup_{X \rightarrow 0} F(X)|X|^n < 1$ and $\liminf_{X \rightarrow \infty} F(X)|X|^n > 1$. In three dimensions we obtain an optimal result, and we also have some partial results in higher dimensions. (Received April 13, 2006)