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Linyuan Lu* (lu@math.sc.edu), Department of Mathematics, LeConte College 1523 Greene Street, University of South Carolina, Columbia, SC 29212. *On a problem of Erdős and Lovász on coloring non-uniform hypergraphs.*

Let $f(r) = \min_H \sum_{F \in E(H)} \frac{1}{2^{|F|}}$, where H ranges over all 3-chromatic hypergraphs with minimum edge cardinality r . Erdős-Lovász (1975) conjectured $f(r) \rightarrow \infty$ as $r \rightarrow \infty$. This conjecture was proved by Beck in 1978. Here we show a new proof for this conjecture with a better lower bound:

$$f(r) \geq \left(\frac{1}{16} - o(1)\right) \frac{\ln r}{\ln \ln r}.$$

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