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*Remarks on the conditionnal regularity of the 3D Navier-Stokes equation.*

We give sufficient conditions for the regularity of Leray-Hopf weak solutions of the Navier-Stokes equation. We prove that if one of three conditions (i)  $\partial u/\partial x_3 \in L_t^{s_0} L_x^{r_0}$  where  $\frac{2}{s_0} + \frac{3}{r_0} \leq 2$  and  $9/4 \leq r_0 \leq 3$ , (ii)  $\nabla u_3 \in L_t^{s_1} L_x^{r_1}$  where  $\frac{2}{s_1} + \frac{3}{r_1} \leq \frac{11}{6}$  and  $54/23 \leq r_0 \leq 18/5$ , or (iii)  $u_3 \in L_t^{s_0} L_x^{r_0}$  where  $\frac{2}{s_0} + \frac{3}{r_0} \leq \frac{5}{8}$  and  $24/5 \leq r_0 \leq \infty$ , then the solution is regular. These conditions improve earlier results on the conditionnal regularity, of the Navier-Stokes equations. This is a joint work with I. Kukavica. (Received September 12, 2006)