

1024-11-187

**Ognian Trifonov\*** ([trifonov@math.sc.edu](mailto:trifonov@math.sc.edu)), Department of Mathematics, LeConte College, 1523 Greene Street, University of South Carolina, Columbia, SC 29208, **Michael Filaseta** ([filaseta@math.sc.edu](mailto:filaseta@math.sc.edu)), Department of Mathematics, LeConte College, 1523 Greene Street, University of South Carolina, Columbia, SC 29208, and **Travis Kidd**. *On the irreducibility of the Laguerre polynomials  $L_m^{(m)}(x)$ .*

The generalized Laguerre polynomials are defined by

$$L_m^{(\alpha)}(x) = \sum_{j=0}^m \frac{(m + \alpha) \cdots (j + 1 + \alpha)(-x)^j}{(m - j)!j!}.$$

Back in the 1930's I. Schur showed that  $L_m^{(1)}(x)$  for odd  $m > 1$ , and  $L_m^{(-m-1)}(x)$  when  $m$  is divisible by 4, have associated Galois group the alternating group  $A_m$ . In the case  $m \equiv 2 \pmod{4}$ , R. Gow proved that  $L_m^{(m)}(x)$  has associated Galois group  $A_m$  too, provided  $L_m^{(m)}(x)$  is irreducible and  $m > 2$ . We finish I. Schur's work by showing that  $L_m^{(m)}(x)$  is irreducible when  $m \equiv 2 \pmod{4}$  and  $m > 2$ . (Received January 08, 2007)