Let $M$ be an infinite module over a commutative ring $R$ with identity. $M$ is said to be a Jónsson module provided every proper submodule of $M$ has smaller cardinality than $M$. Building on results from Gilmer and Heinzer, we state several new results on these modules. In particular, time-permitting, we give a complete description of these modules over a one-dimensional Noetherian ring, a complete description over an arbitrary Noetherian ring assuming the generalized continuum hypothesis, and we give several necessary and sufficient conditions in order for a Jónsson module to be countable. We provide a few applications of these results and state some open problems. (Received January 09, 2007)