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Bernhard Neumann showed that a group is the union of finitely many proper subgroups if and only if it has a finite noncyclic homomorphic image. J.H.E. Cohn defined $s(G)$ to be the smallest integer n such that the group G is the set-theoretic union of n proper subgroups. The question arises what integers n can occur as $s(G)$ for a group G . By a result of M.J. Tomkinson, for solvable groups $s(G)$ is congruent to 1 modulo a prime power, and there is no group with $s(G) = 7$. Cohn showed that $s(G)=10$ and 16 for G the alternating and symmetric group on 5 letters, respectively. Tomkinson conjectured that there are no groups with $s(G) = 11, 13$ or 15 , respectively.

With the help of GAP we determine $s(G)$ for nonsolvable and simple groups in particular. We found that $s(\text{PSL}(2,7)) = 15$. But current evidence supports Tomkinson's conjecture for $n = 11$ and $n = 13$. (Received December 18, 2006)