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Department of Mathematics, Vanderbilt University, Nashville, TN 37240. *On the matching  
extendability of graphs in surfaces.*

A graph  $G$  with at least  $2n + 2$  vertices is said to be  $n$ -extendable if every matching of size  $n$  in  $G$  extends to a perfect matching. It is shown that (1) if a graph is embedded on a surface of Euler characteristic  $\chi$  and the number of vertices in  $G$  is large enough, the graph is not 4-extendable; (2) given  $g > 0$ , there are infinitely many graphs of orientable genus  $g$  which are 3-extendable, and given  $\bar{g} \geq 2$ , there are infinitely many graphs of non-orientable genus  $\bar{g}$  which are 3-extendable; and (3) if  $G$  is a 5-connected triangulation with an even number of vertices which has genus  $g$  and sufficiently large representativity, then it is 2-extendable. (Received January 03, 2007)