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Koen J R Thas* (kthas@cage.UGent.be), Dept. of Pure Mathematics & Computer Algebra, Krijgslaan 281, S22, 9000 Ghent, Belgium. *The p -modular cohomology algebra of finite p -groups, Pauli operators and symplectic forms.*

For a finite p -group P , let

$$H^*(P) = H^*(P, \mathbb{F}_p) = \bigoplus_{i=0}^{\infty} H^i(P, \mathbb{F}_p)$$

be the p -modular cohomology algebra of P .

A theorem of J.-P. Serre states that if P is a p -group which is not elementary abelian, then there exist non-zero elements $u_1, u_2, \dots, u_m \in H^1(P, \mathbb{F}_p)$ such that

$$(*) \quad \prod_{i=1}^m u_i = 0 \text{ if } p = 2 \text{ and } \prod_{i=1}^m \beta(u_i) = 0 \text{ if } p > 2,$$

where β is the Bockstein homomorphism. The smallest integer m such that relation $(*)$ is satisfied is referred to as the *cohomology length* of P , and is usually denoted by $\mathbf{chl}(P)$.

Secondly, M. Saniga and M. Planat recently formulated a conjecture on the geometric structure of complex general Pauli operators of N -qubit Hilbert spaces. A positive answer would have many implications in the field of Quantum Physics.

In my lecture, I want to show how one can see these questions from a symplectic bridge, and elaborate on their solutions. (Received January 22, 2007)