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**Morteza Seddighin\*** (mseddigh@indiana.edu), Indiana University East, 2325 Chester BLVD, Richmond, IN 47374. *Generalizing Holder McCarthy inequality to Normal Operators using Convex Optimization*. Preliminary report.

We use convex optimization techniques to generalize Hölder-McCarthy inequality. Let  $A$  be a positive operator on a Hilbert space  $H$  satisfying  $M \geq A \geq m > 0$ . Also let  $f(t)$  be a real valued convex function on  $[m, M]$  and  $q$  be a real number, then the inequality

$$(f(A)x, x) \leq \frac{(mf(M) - Mf(m))}{(q-1)(M-m)} \left( \frac{(q-1)(f(M) - f(m))}{q(mf(M) - Mf(m))} \right)^q (Ax, x)^q,$$

which holds for every vector  $x$ , under certain restrictions on  $f$  and  $q$ , is called the Hölder-McCarthy inequality. We will generalize the Hölder-McCarthy inequality from positive operators to accretive normal operators. (Received October 26, 2006)