

1026-05-15

**M Brennan, D Gagliardi and M Lewinter\*** ([marty.lewinter@purchase.edu](mailto:marty.lewinter@purchase.edu)), Purchase College (SUNY), Dept. of Natural Science, Purchase, NY 10577. *Irregularizable Graphs*.

A multigraph is a graph with multiple edges between some pairs of vertices. A graph  $G$  of order  $n$  in [1] is called irregularizable if there exists a multigraph  $M$  such that  $G$  is a spanning subgraph of  $M$  and the degree sequence of  $M$  is  $n, n-1, n-2, \dots, 1$ . A graph  $G$  with degree sequence  $d_n, d_{n-1}, \dots, d_2, d_1$  is called degree dominated (DD) if  $d_i \leq i$  for  $1 \leq i \leq n$ . Note that the minimum degree for a DD graph is 1. In [1] and [2], it is shown that all trees are DD. It is also shown there that a DD graph  $G$  of order  $n$  is irregularizable if and only if  $n = 0$  or  $3 \pmod{4}$ . We establish analogous results when the minimum degree  $> 1$ . To this end, a graph  $G$  of order  $n$  is called degree dominated from  $k$  if  $d_i \leq k+i-1$  for  $1 \leq i \leq n$ . A graph  $G$  of order  $n$  is called irregularizable from  $k$  if there exists a multigraph  $M$  such that  $G$  is a spanning subgraph of  $M$  and the degree sequence of  $M$  is  $k+n-1, k+n-2, \dots, k+1, k$ . Given a graph  $G$  which is DD from  $k$ , we present modularity conditions under which  $G$  is irregularizable from  $k$ .

[1] F. Harary D. Gagliardi and M. Lewinter. Which graphs are irregularizable. Unpublished Manuscript. [2] F. Harary D. Gagliardi and M. Lewinter. A lower bound for the number of irregular multigraphs. Graph Theory Notes of New York, XXXI, 1996. (Received December 18, 2006)