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Igor E. Shparlinski* (igor@ics.mq.edu.au), Department of Computing, Macquarie University, North Ryde, Sydney, NSW 2109, Australia. *Distribution of Modular Inverses and Multiples of Small Integers and the Sato–Tate Conjecture on Average.*

We show that, for sufficiently large integers m and X , for almost all $a = 1, \dots, m$ the ratios a/x and the products ax , where $|x| \leq X$, are very uniformly distributed in the residue ring modulo m . This extends some recent results of Garaev and Karatsuba. We apply this result to show that on average over r and s , ranging over relatively short intervals, the distribution of Kloosterman sums

$$K_{r,s}(p) = \sum_{n=1}^{p-1} \exp(2\pi i(rn + sn^{-1})/p),$$

for primes $p \leq T$ is in accordance with the Sato–Tate conjecture. (Received January 29, 2007)