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Thomas W. Cusick, Yuan Li and Pante Stanica* (pstanica@nps.edu), Naval Postgraduate School, Applied Mathematics Department, Monterey, CA 93943. *Counting Balanced Polynomials over Finite Fields.*

Under mild conditions on n, p , we give a lower bound on the number of n -variable balanced symmetric polynomials over finite fields $GF(p)$, where p is a prime number. The existence of nonlinear balanced symmetric polynomials is an immediate corollary of this bound. Furthermore, we conjecture that $X(2^t, 2^{t+1}l - 1)$ are the only nonlinear balanced elementary symmetric polynomials over $GF(2)$, where $X(d, n) = \sum_{i_1 < i_2 < \dots < i_d} x_{i_1} x_{i_2} \cdots x_{i_d}$, and we prove various results in support of this conjecture. (Received January 25, 2007)