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Bo'az B Klartag* (bkartag@princeton.edu), Department of Mathematics, Washington Road, Princeton University, Princeton, NJ 08544. *A central limit theorem for convex sets.*

Suppose X is a random vector, that is distributed uniformly in some n -dimensional convex set. It was conjectured that when the dimension n is very large, there exists a non-zero vector u , such that the distribution of the real random variable $\langle X, u \rangle$ is close to the gaussian distribution. A well-understood situation, is when X is distributed uniformly over the n -dimensional cube. In this case, $\langle X, u \rangle$ is approximately gaussian for, say, the vector $u = (1, \dots, 1) / \sqrt{n}$, as follows from the classical central limit theorem.

We prove the conjecture for a general convex set. Moreover, when the expectation of X is zero, and the covariance of X is the identity matrix, we show that for 'most' unit vectors u , the random variable $\langle X, u \rangle$ is distributed approximately according to the gaussian law. We argue that convexity - and perhaps geometry in general - may replace the role of independence in certain aspects of the phenomenon represented by the central limit theorem. (Received January 18, 2007)